Protein self-association in solution: The bovine β-lactoglobulin dimer and octamer

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(RECEIVED February 13, 2003; FINAL REVISION June 28, 2003; ACCEPTED July 24, 2003)

Abstract
We have used proton magnetic relaxation dispersion (MRD) to study the self-association of bovine β-lactoglobulin variant A (BLG-A) as a function of temperature at pH 4.7 (dimer–octamer equilibrium) and as a function of NaCl concentration at pH 2.5 (monomer–dimer equilibrium). The MRD method identifies coexisting oligomers from their rotational correlation times and determines their relative populations from the associated dispersion amplitudes. From MRD-derived correlation times and hydrodynamic model calculations, we confirm that BLG-A dimers associate to octamers below room temperature. The tendency for BLG-A dimers to assemble into octamers is found to be considerably weaker than in previous light scattering studies in the presence of buffer salt. At pH 2.5, the MRD data are consistent with an essentially complete transition from monomers in the absence of salt to dimers in 1 M NaCl. Because of an interfering relaxation dispersion from nanosecond water exchange, we cannot determine the oligomer populations at intermediate salt concentrations. This nanosecond dispersion may reflect intersite exchange of water molecules trapped inside the large binding cavity of BLG-A.

Keywords: Protein self-association; protein–protein interactions; protein crystallization; bovine β-lactoglobulin; magnetic relaxation dispersion

Bovine β-lactoglobulin (BLG) is the major whey protein in cow’s milk and has served as a model protein for biophysical studies of folding, stability, and self-association (Sawyer and Kontopidis 2000). The dominant genetic variants of BLG, denoted BLG-A and BLG-B, differ in two of the 162 residues. Like other members of the lipocalin family, BLG has a β-barrel fold with a large internal cavity that binds retinol, fatty acids, and other nonpolar molecules (Brownlow et al. 1997; Qin et al. 1998; Uhrínová et al. 2000; Kontopidis et al. 2002). Depending on pH, temperature, and salt concentration, BLG can exist as a monomer, dimer, or octamer (Kumosinski and Timasheff 1966; McKenzie and Sawyer 1967; Sakurai et al. 2001), and it forms amyloid fibrils in the presence of cosolvents such as trifluoroethanol (Gosal et al. 2002) and urea (Hamada and Dobson 2002).

Under physiological conditions (neutral pH and BLG concentration >50 μM), BLG is predominantly dimeric. Although the dimer interface buries only 6% of the monomer surface area, it involves 12 intermolecular hydrogen bonds and 2 ion pairs (Brownlow et al. 1997; Qin et al. 1998), and these specific interactions have been shown to be critical for dimer stability (Kobayashi et al. 2002; Sakurai and Goto 2002). At pH 2 to 3, at which the protein has a net charge of ~+20, BLG is essentially monomeric under salt-free conditions (Timasheff and Townend 1961b; Baldini et al. 1999; Sakurai et al. 2001). Addition of salt screens the electrostatic repulsion and increases the dimer population.

Below room temperature in the pH range 3.7 to 5.2, BLG reversibly forms a larger oligomer (Townend and Timasheff 1960; Townend et al. 1960; Timasheff and Townend 1961a; Kumosinski and Timasheff 1966; McKenzie et al. 1967; Piazza and Iacopini 2002). This self-association process has a maximum around pH 4.6, just below the isoelectric point, and is more pronounced for BLG-A than for BLG-B, again indicating essential involvement of specific interactions. Static light scattering data indicated that the large oligomer
is a cooperatively formed octamer (Townend and Timasheff 1960; Timasheff and Townend 1961a), and the radius of gyration, deduced from small-angle X-ray scattering (SAXS), indicated a compact cubic arrangement of eight monomers (Timasheff and Townend 1964; Witz et al. 1964). A subsequent static light scattering study indicated that intermediate oligomers (tetramers and hexamers) are present in significant amounts at 8°C and 15°C and at BLG concentrations of <1 mM (Kumosinski and Timasheff 1966). From a more recent static and dynamic light scattering study, it was concluded that the effects of oligomerization and other interparticle interactions cannot be separated (Piazza and Iacopini 2002).

The aim of the present work is to shed new light on BLG self-association by using a different experimental technique: magnetic relaxation dispersion (MRD). Within the biomolecular field, MRD has previously been used mostly to study protein hydration and, in particular, internal water molecules in proteins and nucleic acids (Halle et al. 1999; Halle and Denizov 2001). In a recent study of the BPTI decamer, we have demonstrated that water 1H field-cycling MRD can also yield quantitative information about protein self-association in solution (Gottschalk et al. 2003). Under favorable conditions, MRD yields the rotational correlation times and fractional populations of all oligomeric species present in solution. Large oligomers can be detected even at low (<1%) populations, and the method is independent of the association/dissociation kinetics. Because the rotational correlation time is insensitive to long-range interactions, it reflects the true oligomerization state. Moreover, the oligomer species can be identified by comparing the MRD results with hydrodynamically calculated rotational correlation times for detailed oligomer models.

Water 1H and 2H relaxation data from BLG solutions have been reported previously, but only at a single resonance frequency (Kumosinski and Pessen 1982; Pessen et al. 1985; Kumosinski et al. 1991). It is then not possible to separate correlation times and amplitudes for the different oligomeric species. In contrast, our relaxation data span more than four orders of magnitude in frequency. We focus on the temperature-dependent dimer–octamer equilibrium at pH 4.7, but we also report results on the salt-dependent monomer–dimer equilibrium at pH 2.5. We also show that MRD is a sensitive probe of protein purity, revealing a significant population of very large oligomers present even after purification by anion exchange chromatography. Removal of these aggregates by gel filtration is essential in studies of self-association.

**Results and Discussion**

**Temperature-dependent dimer–octamer equilibrium**

The dimer–octamer equilibrium was studied at pH 4.7 in the absence of buffer or added salt and at BLG concentrations of 0.74 to 0.84 mM. Under these conditions and at 27°C, virtually all BLGs should exist in dimeric form (McKenzie and Sawyer 1967). On lowering the temperature, we observe a strong enhancement of the 1H relaxation rate at low frequencies and a low-frequency shift of the dispersion region (Fig. 1). These changes indicate increased correlation times. According to the Stokes-Einstein-Debye relation, the rotational correlation time (τ) is proportional to η(T)/T, where η is the temperature-dependent viscosity of the aqueous solvent. If the size and shape of the protein does not change with temperature, we may write τ(η) = γτ(η0), with a dynamic scaling factor γ = T0 η(T)/T η(η0). Taking T0 = 300 K as the reference temperature, we have γ = 2.226 at 274 K. However, the low-frequency 1H relaxation rate R0 increases by more than a factor five on going from 300 to 274 K (Fig. 1). We can thus conclude that the protein structure, or oligomerization state, depends strongly on temperature.

All the dispersion profiles in Figure 1 exhibit a small-amplitude dispersion step at frequencies ~10^8 Hz. This frequency corresponds to a correlation time of ~1 nsec, an order of magnitude shorter than the rotational correlation of the BLG dimer (or monomer). This dispersion step must therefore be attributed to water molecules with residence times of ~1 nsec (see below). The main dispersion step, which reflects the rotational diffusion of BLG oligomers, is broadened at low temperatures and cannot be reproduced with a single rotational correlation time. This qualitative observation indicates that more than one oligomer species is present at low temperatures.

![Figure 1](https://www.proteinscience.org)  
1H relaxation dispersion profiles from aqueous BLG solutions at pH 4.7 (no buffer and no added salt) and temperatures from 1°C to 27°C. The data have been normalized to 1.00 mM BLG. The correlation curves resulted from a joint fit according to equations 1 and 2 with N = 2. The three correlation times were constrained to scale with temperature as η(T)/T.
To determine the size and relative population of the oligomers, we fitted the theoretical relaxation dispersion expression (equations 1, 2) to the relaxation data in Figure 1. Three correlation times are needed to reproduce the data to within the experimental accuracy (as judged by the F test): a water residence time τ_0 and two rotational correlation times, τ_1 and τ_2. If the temperature variation alters the oligomer populations without changing the oligomer structures, it should be possible to fit all four dispersion profiles jointly to three correlation time parameters, which we choose as τ_0, τ_1, and τ_2 at 300 K. The correlation times at the other temperatures are then obtained from the relation τ_0(T) = γτ_0(T_0) with known scaling factors γ (Table 1). The excellent fit (χ^2 = 1.8) in Figure 1 supports this reasonable assumption.

The correlation times deduced from the fit are τ_0 = 0.65 ± 0.11 nsec, τ_1 = 20.4 ± 0.9 nsec, and τ_2 = 111 ± 3 nsec, all at 300 K. The rotational correlation time of the BLG-A monomer has been determined to 7.30 ± 0.05 nsec, all at 300 K. The rotational correlation time of the BLG-B dimer (Protein Data Bank [PDB] code 1BSY with hydrogen atoms added). For the octamer, studied at pH 4.5 (100 mM acetate buffer) and 3°C, the SAXS study yielded R_G = 34.4 ± 0.4 Å (Witz et al. 1964). This was shown to be consistent with a cubic array of eight spheres (Timasheff and Townend 1964; Witz et al. 1964). For such an array, hydrodynamic calculations yield τ_0(octamer)/τ_0(monomer) = 1.0/0.075 (García de la Torre and Bloomfield 1981). Combining this with the experimentally derived τ_0(monomer) value quoted above, we obtain τ_0(octamer) = 121 nsec at 300K. This is only 10% from the MRD-derived correlation time τ_2 and, given that the hydrodynamic model lacks atomic detail, strongly indicates that the low-frequency component of the dispersion profile is produced by a BLG octamer with the cubic structure deduced from SAXS data.

Fluorescence depolarization on 1.1 mM BLG-A at pH 4.6 (100 mM acetate buffer) and 2°C yielded a rotational correlation time of 65 nsec after scaling to 300 K (Wahl and Timasheff 1969). This much smaller value was deduced under the assumption that the BLG solution was monodisperse. However, a substantial dimer population should be present under these conditions (see below). The correlation time deduced from fluorescence depolarization should therefore be an effective one, reflecting both dimers and octamers. In contrast, MRD data allow the rotational diffusion of dimer and octamer to be resolved. It should be noted that even if a substantial dimer population were present in the SAXS study discussed above, the observed radius of gyration would not deviate much from that of the more massive octamer.

Having identified the oligomeric species as dimer and octamer, we can now determine their relative populations from the mean-square fluctuation amplitudes b_1 and b_2 derived from the fit (see equation 1). These amplitudes can be expressed as b_n = x_n β_n, where x_n is the fraction of BLG molecules that belong to the nth oligomer species or, equivalently, the weight fraction of that species (Gottschalk et al. 2003). The intrinsic mean-square fluctuation amplitude β_n is proportional to the number of protons (per BLG monomer) with residence times long enough (τ_1 < τ_2) to sample the rotational diffusion of the oligomer but short enough (<1/[β_n τ_2]) to act as a relaxation sink for the observed water 1H magnetization (Halle et al. 1999; Halle and Denisov 2001). We assume that the number of internal water molecules and rapidly exchanging labile hydrogens are the same (on a monomer basis) in the dimer and the octamer. At each temperature, we then have β_1 = β_2, and it follows that the fractional populations can be obtained as x_n = b_n/B, where B = b_1 + b_2. If this assumption is correct, B should be independent of the oligomer fractions, but it may depend on temperature. As seen from Table 1, B is nearly constant at the three higher temperatures but is sub-

<table>
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<tr>
<th>T (°C)</th>
<th>C_p^a (mM)</th>
<th>γ</th>
<th>β</th>
<th>x_octamer</th>
<th>ΔG^d</th>
<th>R_G (Å)</th>
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<tr>
<td>1.0</td>
<td>0.84</td>
<td>2.226</td>
<td>1.28 (3)</td>
<td>0.20 (4)</td>
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<td>7.0</td>
<td>0.82</td>
<td>1.797</td>
<td>0.73 (3)</td>
<td>0.18 (4)</td>
<td>-49 (1)</td>
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<tr>
<td>14.0</td>
<td>0.82</td>
<td>1.435</td>
<td>0.80 (4)</td>
<td>0.16 (4)</td>
<td>-50 (1)</td>
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<tr>
<td>27.0</td>
<td>0.74</td>
<td>1</td>
<td>0.68 (5)</td>
<td>0.03 (2)</td>
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<th>a</th>
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<td>b</td>
<td>Dynamic scaling factor. γ = 300 η(T)/[η(300 K)].</td>
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<td>c</td>
<td>Total fluctuation amplitude. β = b_1 + b_2, normalized to C_p = 1.00 mM.</td>
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<td>d</td>
<td>Uncertainty in last position given within parentheses.</td>
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At nearly constant at the three higher temperatures but is sub-
stantially larger at 274 K. This might reflect a low-temperature structural change in BLG that traps additional hydration water molecules. In this connection, it is interesting to note that monomeric BLG-A at pH 2.0 to 2.5 has been shown to undergo cold-denaturation in the presence of urea (Griko and Privalov 1992; Griko and Kutyshenko 1994; Katou et al. 2001).

The analysis of our MRD data shows that the octamer fraction increases from 0.03 at 300 K to 0.20 at 274 K (Table 1). From the octamer fraction \( x_{\text{octamer}} \equiv x_2 \), we may calculate a stoichiometric association constant for an octamer formed with full cooperativity as \( K_{\text{octamer}} = \frac{x_{\text{octamer}}}{(1 - x_{\text{octamer}})C_P} \), where \( C_P \) is the total BLG concentration on a monomer basis. The associated standard free energy of association, calculated as \( \Delta G_{\text{octamer}}^\circ = -RT \ln K_{\text{octamer}} \) is remarkably constant at \( -49 \pm 1 \) kJ mole\(^{-1}\) over the investigated temperature range (Table 1). Static light scattering studies of BLG-A at pH 4.65 (100 mM acetate buffer) yielded \( \Delta G_{\text{octamer}} = -48.9 \) kJ mole at 298 K (Kumosinski and Timasheff 1966), in good agreement with our result. However, these investigators found that \( \Delta G_{\text{octamer}} \) varies linearly with temperature, reaching \(-64.4 \) kJ mole\(^{-1}\) at 274 K. This would correspond to an octamer fraction of 0.80 in our 274 K sample, four times higher than what we obtained. Such a high octamer fraction is definitely ruled out by our data. However, these investigators found that \( \Delta G_{\text{octamer}} \) varies linearly with temperature, reaching \(-64.4 \) kJ mole\(^{-1}\) at 274 K. This would correspond to an octamer fraction of 0.80 in our 274 K sample, four times higher than what we obtained. Such a high octamer fraction is definitely ruled out by our data.

The monomer–dimer equilibrium was studied at pH 2.5 and 300 K in the presence of 0, 0.010, 0.050, or 1.00 M added NaCl. We note that the “no salt” sample has an ionic strength of 15 to 20 mM due to the chloride ions added with the HCl used to adjust the pH. The BLG concentration was 0.71 to 1.00 mM. With increasing salt concentration, we observed a monotonic increase of the dispersion amplitude and a low-frequency shift of the dispersion, indicating salt-induced formation of larger, more slowly tumbling oligomers. This is shown in Figure 2 for the two extreme cases. The salt effect at pH 2.5 is much smaller than the effect of temperature at pH 4.7 (note the different \( R_1 \) scales in Figs. 1 and 2). As a result, the high-frequency dispersion step from water molecules with nanosecond correlation times now makes a larger relative contribution to the dispersion profile. Moreover, the rotational correlation times of the BLG-A monomer and dimer only differ by a factor of 2.26 (see Materials and Methods), making it difficult to resolve the individual Lorentzian contributions to the dispersion.

![Figure 2. \(^1\)H relaxation dispersion profiles from aqueous BLG solutions at pH 2.5 (no buffer) and 27°C without added salt and in the presence of 1 M NaCl. The data have been normalized to 1.00 mM BLG. The dispersion curves resulted from a joint fit according to equations 1 and 2 with \( N = 2 \) and frozen correlation times (see text).](http://www.proteinscience.org)
In an attempt to overcome these problems, we fitted the no salt and 1 M NaCl dispersions with the three correlation times fixed. The water correlation time $\tau_0$ was taken as 0.65 nsec, as obtained (at 300 K) from the fit to the pH 4.7 MRD data, in which this dispersion step is better resolved due to absence of BLG monomers. The monomer correlation time $\tau_1$ was set to 9.1 nsec, as determined by $^{15}$N relaxation (Uhrínová et al. 2000), and the dimer correlation time $\tau_2$ was set to 20.4 nsec, as obtained (at 300 K) from the pH 4.7 MRD data and also from hydrodynamic calculations (see above). For the 1 M NaCl solution, these correlation times were multiplied by a factor 1.095, accounting for the higher bulk solvent viscosity. As seen from Figure 2, the dispersion profiles are well described by these correlation times.

As for the pH 4.6 MRD data, we can determine the dimer fraction $x_{\text{dimer}} = x_2$ from the mean-square fluctuation amplitudes $b_n = x_n \beta_n$, assuming that $\beta_1 = \beta_2$. As required if this assumption is correct, $B = b_1 + b_2$ does not vary significantly with salt concentration: $B = (0.65 \pm 0.06) \times 10^7$ sec$^{-2}$ in the absence of salt and $(0.7 \pm 0.1) \times 10^7$ sec$^{-2}$ in 1 M NaCl. This analysis yields $x_{\text{dimer}} = 0$ in the absence of salt (this dispersion profile is thus modeled with only two Lorentzians) and $x_{\text{dimer}} = 0.4 \pm 0.1$ in 1 M NaCl. Previous studies of the monomer–dimer equilibrium of BLG-A at pH 2.3 to 3.0 by sedimentation, light scattering, and SAXS indicate that at pH 2.5, 300 K, and 1 mM BLG, $x_{\text{dimer}} = 0.1$ in the absence of added salt and $x_{\text{dimer}} = 0.9$ in 1 M NaCl (Timasheff and Townend 1961b; Tang and Adams 1973; Baldini et al. 1999; Sakurai et al. 2001). Whereas our results agree with previous work in the absence of salt, there is a substantial discrepancy at 1 M NaCl. This can be resolved as follows.

A statistical analysis (using the $F$ test) shows that the 1 M NaCl data are reproduced within experimental accuracy by two Lorentzians. Without fixing correlation times, these data therefore cannot be used to establish coexisting monomer and dimer populations. The dimer fraction derived from the tri-Lorentzian fit in Figure 2 depends on the values assigned to the fixed correlation times. Whereas the monomer and dimer rotational correlation times $\tau_1$ and $\tau_2$ are accurately known, the value of the water-exchange correlation time $\tau_0$ is less certain. To test if our data are consistent with previous results for the dimer fraction, we thus performed bi-Lorentzian fits with $\tau_0$ freely adjustable but $\tau_1$ (no salt) and $\tau_2$ (1 M NaCl) fixed as before. The resulting fits are virtually indistinguishable from those shown in Figure 2, but now $\tau_0 = 3$ nsec. Considering that the net charge of BLG is much higher at pH 2.5 (+20) than at pH 4.7 (+4), such a pH dependence in $\tau_0$ cannot be ruled out. We therefore conclude that the present MRD data are consistent with previous results (Timasheff and Townend 1961b; Tang and Adams 1973; Baldini et al. 1999; Sakurai et al. 2001), indicating that under our conditions, BLG is almost completely monomeric in the absence of salt and almost completely dimeric in 1 M NaCl.

Finally, we note that the 1 M NaCl dispersion shows a small low-frequency step (below the frequency range of Fig. 2) corresponding to a correlation time of $1.0 \pm 0.3$ µsec. This indicates that small amounts of very large BLG aggregates form at high salt concentration, despite the high structural charge of BLG at pH 2.5.

Conclusions

The self-association of bovine BLG has been extensively studied by several physical techniques in the past. Whereas the salt-dependent monomer–dimer equilibrium at pH 2 to 3 has been characterized in considerable detail, the temperature-dependent dimer–octamer equilibrium near the isoelectric point is not as well understood. In particular, a high-resolution structure of the octamer is not available.

Here, we have used proton MRD to shed further light on the dimer–octamer equilibrium of BLG-A at pH 4.7. The MRD data reveal two oligomeric species with rotational correlation times of 20.4 ± 0.8 nsec and 111 ± 3 nsec at 27°C. The shorter correlation time agrees with the dimer correlation time, 20.5 ± 0.1 nsec, predicted on the basis of the monomer correlation time determined by $^{15}$N spin relaxation (Uhrínová et al. 2000) and our hydrodynamic calculations on the monomer and dimer crystal structures. The longer correlation time is consistent with a crude theoretical estimate, 121 nsec, based on the cubic arrangement of eight monomers predicted from SAXS data (Timasheff and Townend 1964; Witz et al. 1964).

Whereas the MRD data confirm that BLG-A self-associates to dimers and octamers at pH 4.7, they differ from previously reported light scattering results with regard to the relative populations of these oligomeric species. Reasonable agreement is found at 27°C, but we obtain a significantly lower octamer fraction at 1°C. This difference may be caused by the presence of buffer salt in all previous studies, which should promote octamer formation by electrostatic screening.

We have also used MRD to study the monomer–dimer equilibrium at pH 2.5 as a function of NaCl concentration. The MRD data are consistent with an essentially monomeric protein in the absence of salt and an essentially dimeric protein in 1 M NaCl, with the expected rotational correlation times for the monomer and dimer. However, because of the presence of an additional dispersion step from water molecules with nanosecond correlation time, it is not possible to resolve the monomer and dimer contributions in a unique way. Because this nanosecond correlation time is shorter than the rotational correlation time of the BLG monomer, it must reflect water motions. Water correlation times in this range have previously been associated with the exchange of water molecules from singly occupied deep
surface pockets in several proteins (Halle 1999) and with inter-site exchange among the ∼20 water molecules trapped inside the internal cavity of a fatty acid binding protein (Wiesner et al. 1999). Few, if any, water molecules have been crystallographically localized within the internal binding cavity of BLG. However, positional disorder could make such water molecules difficult to observe at the resolution of the current BLG structures (Brownlow et al. 1997; Qin et al. 1998; Kontopidis et al. 2002). Further MRD work, with more extensive data at high frequencies, would be required to obtain reliable information about the number of water molecules responsible for the nanosecond dispersion. Difference-MRD experiments with a bound ligand, such as retinol, should also be useful in this regard.

Materials and methods

Protein purification

BLG-A, prepared from the milk of homozygous cows at the INRA Laboratoire de Recherche de Technologie Laitière, was generously supplied by Dr. C. Holt of the Hannah Research Institute (Ayr, Scotland). A second batch of BLG-A was purchased from Sigma (L-7880, lot no. 70K7049). Both protein preparations were first purified by anion exchange chromatography at pH 6.0 (10 mM MES buffer) on a DEAE-sephacel column, eluted with a 25 to 300 mM NaCl gradient. Although the purified protein preparations yielded a single band in agarose gel electrophoresis and SDS-PAGE, ~1% of high-molecular-weight species (probably a BLG polymer) was detected in both preparations by MRD at pH 2.5 (Fig. 3). To remove this impurity, we further purified the INRA preparation by gel filtration at pH 2.7 (10 mM citric acid, 50 mM NaCl) on a Sephadex G-50 column. The protein was then dialyzed against milli-Q water and lyophilized. All MRD data reported here (except profiles 1 and 2 in Fig. 3) were measured on samples made from this preparation.

Preparation of MRD samples

MRD samples were made by dissolving the purified protein in oxygen depleted water (<0.001% O₂, Fluka BioChemika). The pH value, which was 4.6 to 4.7 after dissolution, was adjusted by microliter additions of HCl. No buffers were used. All quoted pH values were measured at room temperature. For the salt series, desiccator dried NaCl (≥99.5%, Merck) was added, whereupon the solution was centrifuged at 14,000 rpm for 3 min to remove a small fraction of aggregated material. Protein concentrations were determined spectrophotometrically (Shimadzu UV-1601) at 278 nm by using an extinction coefficient of 1.11 mL mg⁻¹ cm⁻¹, determined from quantitative amino acid analysis on two samples. To remove paramagnetic oxygen, the solution was gently bubbled with argon gas during 4 h, whereupon the 10-mm NMR tube was sealed with a septum. With this procedure, the ¹H relaxation rate in a pure water sample was found to be 0.267 ± 0.008 sec⁻¹, in agreement with the standard literature value of 0.266 sec⁻¹ (Hindman et al. 1973), and remained within 1% of this value for at least 10 d.

Relaxation dispersion measurements

The longitudinal relaxation of the water ¹H resonance was studied from 10 kHz to 200 MHz by using (1) a Stelar Spinnmaster fast field-cycling (FC) spectrometer (20 kHz to 6 MHz), (2) a field-variable iron-core magnet (Drusch) equipped with a Tecmag Discovery console (10 to 78 MHz), and (3) Bruker Avance DMX 100 and 200 spectrometers with conventional cryomagnets (100.1 and 200.1 MHz). The temperature was maintained to within ±0.1°C using a Stelar variable temperature control unit (< 100 MHz) or a Bruker Eurotherm regulator (at 100 and 200 MHz). Temperatures were checked by using a thermocouple referenced to an ice-water bath.

The longitudinal relaxation rate ¹R₁ was measured with the inversion recovery method (fixed-field experiments) and by the pre-polarized (≪4 MHz) or non-polarized (≫4 MHz, avoiding short evolution times) FC protocols. The small contribution from non-exchanging protein protons was eliminated by selective integration (fixed field) or by delayed acquisition (FC). All other details of the relaxation experiments were as previously described (Gottschalk et al. 2003). The accuracy in ¹R₁ is estimated to ±1% at the two highest fields and 1% to 2% (1 SD) at the other fields.

Analysis of relaxation dispersion data

The measured ¹H relaxation rate is due to thermal fluctuations of intramolecular and intermolecular magnetic dipole–dipole couplings experienced by water protons and labile BLG protons in fast or intermediate exchange (residence time <10 msec, typically) with the water protons (Halle et al. 1999; Halle and Denizov 2001). The relaxation dispersion, that is, the frequency dependence of ¹R₁, is produced by long-lived (residence time 10⁻³ to 10⁻² sec) water molecules in intimate association with the protein and by labile protons with residence times in the same range. The dispersion

![Figure 3. ¹H relaxation dispersion profiles from aqueous 1 mM BLG solutions at 27°C and pH 2.5. The protein source and purification level for the three profiles are as follows: (1) Sigma, anion exchange chromatography (diamonds); (2) INRA, anion exchange chromatography (filled circles); and (3) INRA, anion exchange chromatography followed by gel filtration (open circles). Dispersion steps <1 MHz in cases 1 and 2 are due to 1.0 ± 0.5% of high-molecular-weight impurity with correlation time 0.25 ± 0.06 μsec (INRA) and 0.82 ± 0.05 μsec (Sigma) as deduced from the depicted tri-Lorentzian fits with the intermediate correlation time frozen to 9.1 nsec (as expected for the monomer). The solvent of sample 2 contained 25 vol% D₂O.](image-url)
profile, $R_1(\omega_0)$, from a solution containing BLG in $N$ different oligomeric states is described by the following relations (Halle et al. 1999; Halle and Denisyov 2001)

$$R_1(\omega_0) = \alpha + b_\alpha (L(\omega_0, \tau_\alpha)) + \sum_{n=1}^{N} b_n L(\omega_0, \tau_n)$$

(1)

$$L(\omega_0, \tau_n) = \frac{0.2\tau_\alpha}{1 + \left(\frac{\omega_0\tau_\alpha}{2}\right)^2} + \frac{0.8\tau_\alpha}{1 + \left(2\omega_0\tau_\alpha\right)^2}$$

(2)

Here, $b_n$ and $\tau_n$ are the mean-square fluctuation amplitude and correlation time, respectively, associated with the $n$th dispersion step. The correlation time $\tau_n$ is related to the BLG oligomer rotational correlation time $\tau_{R,n}$ and the mean proton residence time $\tau_{L,n}$ as (Halle et al. 1999)

$$\frac{1}{\tau_n} = \frac{1}{\tau_{R,n}} + \frac{1}{\tau_{L,n}}$$

(3)

Labile protons generally have residence times much longer than the protein rotational correlation time and therefore do not contribute to $\tau_n$. This is usually the case also for protons in deeply buried internal water molecules. However, water molecules in deep surface pockets or trapped in large internal cavities may have site residence times in the range of 1 to 10 nsec (Halle 1999; Wiesner et al. 1999) and will then shorten the correlation time $\tau_n$ according to equation 3. All our MRD profiles from BLG solutions show a dispersion step with a correlation time of ~1 nsec, attributable to such water molecules. This contribution is modeled by the second term in equation 1, which, for simplicity, is represented by a single correlation time. Our main focus here is on the dispersion steps $n = 1, 2, ..., N$ that report on the oligomeric species of BLG (monomer, dimer, or octamer). The correlation time $\tau_n$ can be identified with the isotropic rotational correlation time $\tau_R$ of the $n$th oligomer species, and the amplitude $b_n$ allows its fractional population to be determined.

For brevity, the functions $L(\omega_0, \tau_n)$ will be referred to as Lorentzians, even though they contain two Lorentzian components. In the analysis of MRD data, we actually used a more involved dispersion function, which is a linear combination of the intramolecular dispersion function in equation 2 and an intermolecular dispersion function (Abragam 1961; Halle et al. 1999). The relative weight of the intermolecular function was set to 0.33 (Venu et al. 1997), but any value in the allowed range of 0 to 1 could be used without significantly affecting the correlation times and amplitudes deduced from the fits. The parameter $\alpha$ in equation 1 represents all frequency-independent contributions to the measured relaxation rate, including bulk water, rapidly exchanging ($\tau_R \ll 1$ nsec) surface waters, and the secular (zero-frequency) intermolecular contribution from internal waters and labile BLG protons (Venu et al. 1997). Because of incomplete characterization of the highest-frequency dispersion step (with a correlation time of ~1 nsec), the $\alpha$ parameter could not be determined with useful accuracy. The dispersion profiles are therefore displayed with the small frequency-independent contribution subtracted and with the frequency-dependent part normalized to the same BLG concentration (Gottschalk et al. 2003):

$$R_1^{\text{norm}} = (R_1 - \alpha) N_T / \lambda_T^{\text{norm}}$$

(4)

where $N_T$ is the number of water molecules per BLG monomer in the solution and $N_T^{\text{norm}}$ was taken as 55,000, corresponding to a BLG monomer concentration of 1.00 mM.

The experimental relaxation dispersion data were subjected to nonlinear Marquardt-Levenberg $\chi^2$ minimization (Press et al. 1992) with the model function given by equations 1 and 2. This fit involves the $2N + 1$ parameters $\alpha$, $b_n$, $\tau_n$, and $\tau_R$ with the products $b_n\tau_n$ constrained to be nonnegative. The number $N$ of Lorentzians to be included in the fit was determined objectively by the $F$ test with a cutoff probability of 0.9 (Press et al. 1992; Halle et al. 1998). The dispersions were thus found to be adequately modeled by two Lorentzians ($N = 2$) in addition to the nanosecond water dispersion ($n = 0$). For each of the two sets of experiments (salt dependence and temperature dependence), the dispersion profiles were fitted jointly under the assumption that the same oligomers are present under all conditions but with different relative populations. Quoted uncertainties in the fitted parameter values correspond to 1 SD and were obtained by the Monte Carlo method (Press et al. 1992) using 1000 synthetic data sets.

**Hydrodynamic calculations of rotational correlation times**

The rotational correlation times $\tau_1$ and $\tau_2$ obtained from the MRD data contain information about oligomer size and shape. To verify our assignments of oligomer species, we carried out hydrodynamic calculations of the rotational diffusion tensor $D_R$ of BLG-A with the program HYDROPRO, version 5.0 (García de la Torre et al. 2000). In these calculations, each nonhydrogen atom in a crystallographic model of the protein is replaced by a spherical bead of radius $\sigma$. The shell of beads remaining after all internal beads have been deleted is then filled with smaller spheres of radius $\sigma$ that act as point sources of hydrodynamic friction. The rotational diffusion tensor $D_R$ is computed as a function of $\sigma$ and extrapolated to $\sigma = 0$ (García de la Torre and Bloomfield 1981). The rank-2 isotropic rotational correlation time is defined as $\tau_0 = (2 \pi D_R)^{-1}$. Because macroscopic continuum hydrodynamics is not strictly valid on the atomic scale, this calculation does not necessarily yield results in quantitative agreement with experiment. The approach usually adopted is to regard the bead radius $\sigma_b$ as an empirical parameter (rather than using the van der Waals radii of the actual atoms), the value of which is determined by requiring that the calculation agrees with the experimental value of a particular hydrodynamic quantity, such as $\tau_0$ (García de la Torre et al. 2000).

Our calculations are based on the crystal structure 1BSY of BLG-A at 298 K (pH 7.1) determined at 2.24 Å resolution in the trigonal space group P 321 with six asymmetric units per unit cell (Qin et al. 1998). For calculations on the monomer, we used the atomic coordinates deposited in the PDB file (which includes all 162 residues). For the dimer, we generated the other subunit by the crystallographic symmetry operations given in the PDB file (molecule 6). For monomeric BLG-A, we calculated $\tau_0$ at 27°C for $\sigma_b$ values in the range of 1.0 to 4.0 Å. Interpolation at the experimental value $\tau_0 = 9.09 \pm 0.06$ nsec (Uhrinová et al. 2000) yields $\sigma_b = 2.97 \pm 0.04$ Å. We then used this bead radius to calculate the ratio of the rotational correlation times for the BLG-A dimer and monomer, obtaining $\tau_0(\text{dimer}) / \tau_0(\text{monomer}) = 2.26$. This ratio is quite insensitive to the bead radius, varying by only 0.15 over the range $\sigma_b = 1.0$ to 4.0 Å.

For a general asymmetric top, the dispersion function (or spectral density) involves five rotational correlation times. The BLG-A monomer, however, is very nearly spherical, and the ratio of the longest and shortest rotational correlation times is 1.08. The dimer is better described as a prolate symmetric top, but the correlation time ratio of 1.45 is not large enough to produce a significant
deviation from spherical top behavior in the MRD profile. Accordingly, we describe both monomer and dimer with single (isotropic) rotational correlation times.

Acknowledgments

We thank Hans Lilja and Vladimir Denisov for spectrometer assistance and Peter Sellers for helpful suggestions. This work was supported by the Swedish Research Council and the Crafoord Foundation.

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